OPTIMAL DESIGN OF ARCH DAMS FOR FREQUENCY LIMITATIONS USING CHARGED SYSTEM SEARCH AND PARTICLE SWARM OPTIMIZATION

A. Kaveh and V.R. Mahdavi
Centre of Excellence for Fundamental Studies in Structural Engineering, Iran University of Science and Technology, Narmak, Tehran-16, Iran

ABSTRACT

In recent years, the importance of economical considerations in the field of dam engineering has motivated many researchers to propose new methods for minimizing the cost of dams and in particular arch dams. This paper presents a method for shape optimization of double curvature arch dams corresponding to minimum construction cost while satisfying different constraints such as natural frequencies, stability and geometrical limitations. For optimization, the charged system search (CSS) and particle swarm optimization (PSO) are employed. To validate the finite element model, a real arch dam is considered as a test example. The results of the present method are compared to those of other optimization algorithms for the selected example from literature.

Received: 20 August 2011; Accepted: 28 December 2011

KEY WORDS: Arch dam; natural frequency; charged system search; particle swarm optimization

1. INTRODUCTION

In recent decades, the researchers have focused on optimization of concrete arch dams because of the high construction cost and damage caused by these structures. The main objective of this research is to find a shape of arch dams that has minimum volume or cost while satisfying the corresponding constraints. One of the most important constraints is the behavior constraint. On other hand, natural frequencies are fundamental parameters which

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*Corresponding author: A. Kaveh, Centre of Excellence for Fundamental Studies in Structural Engineering, Iran University of Science and Technology, Narmak, Tehran-16, Iran
†E-mail address: alikaveh@iust.ac.ir
affect dynamic behavior of the arch dams. Therefore, some limitations should be imposed on the natural frequency range to reduce the domain of vibration and also prevent the resonance phenomenon in dynamic response of arch dams. Traditionally, an arch dam is iteratively analyzed and designed to achieve this goal [1].

Recently some progress has been made in optimum design of arch dams considering different constraints. Almost all of these have used conventional methods for analysis approximation and optimization. These methods usually employ derivative calculations and may be trapped in local optima. The shape optimization of arch dams has been developed after appearing and development of finite element method in late 1950’s. Early research works dealt mainly with membrane-type solutions [2]. Later, Rajan [3], Mohr [4] and Sharma [5] developed solutions based on membrane shell theory. Sharpe [6] was the first to formulate the optimization as a mathematical programming problem. A similar method was also adopted by Rickeets and Zienkiewicz [7] who used finite element method for stress analysis and Sequential Linear Programming (SLP) for the shape optimization of arch dams under static loading.

An optimization problem may be solved by a global search optimization method including both probabilistic and deterministic concepts without any dependency on the gradients or derivatives of functions in searching for the optimal global solution. Unfortunately the gradient/derivative-based optimization methods have a tendency to be trapped in local minima for problems with a complex search domain. The charged system search (CSS) is one of the newly developed meta-heuristic algorithms which has been utilized for optimum design of different types of structures, Kaveh and Talatahari [8]. The governing laws from the physics initiate the base of the CSS algorithm. Particle swarm optimization (PSO) is another meta-heuristic algorithm widely utilized for optimization problems due to its simple principle and ease of implementation, Eberhart and Kennedy [9].

In this study, the CSS and PSO algorithms are employed for cost optimization of arch dams. The arch dam cost consisting of the concrete volume and the casting areas is considered as the objective function. The design variables are geometric parameters of the arch dam. To implement a practical design optimization, many constraints such as stress, displacement, stability requirement, and frequency constraints should be considered. In the present study, for simplicity of the optimization operation and comparison with the existing results from literature, only frequency and some geometrical constraints are considered. The Opensees [10] and Matlab [11] are used for modeling, modal analysis and calculation the cost of the arch dam, respectively.

The results of the solved examples demonstrate that CSS leads to better results than PSO. Also the results of these algorithms are better than those of the previously developed algorithms.

2. CHARGED SYSTEM SEARCH ALGORITHM

2.1. The standard Charged Search System

The Charged System Search is a population-based search approach, where each agent (CP) is considered as a charged sphere with radius \( r \), having a uniform volume charge density which can produce an electric force on the other CPs. The force magnitude for a CP located inside the sphere is proportional to the separation distance between the CPs, while for a CP located...
outside the sphere it is inversely proportional to the square of the separation distance between the particles. The resultant forces or acceleration and the motion laws determine the new location of the CPs. The pseudo-code for the CSS algorithm can be summarized as follows:

**Step 1: Initialization.** The initial positions of CPs are determined randomly in the search space and the initial velocities of charged particles are assumed to be zero. The values of the fitness function for the CPs are determined and the CPs are sorted in an increasing order. A number of the first CPs and their related values of the fitness function are saved in a memory, so called charged memory (CM).

**Step 2: Determination of the forces on CPs.** The force vector is calculated for each CP as

\[
F_j = \sum_{i \neq j} \left( \frac{q_i}{r_{i,j}} \right)^2 \cdot ar_{i,j} \cdot p_{i,j} \cdot (X_i - X_j) \]

where \(F_j\) is the resultant force acting on the \(j\)th CP; \(N\) is the number of CPs. The magnitude of charge for each CP (\(q_i\)) is defined considering the quality of its solution as

\[
q_i = \frac{\text{fit}(i) - \text{fitworst}}{\text{fitbest} - \text{fitworst}}, \quad i = 1,2,\ldots,N
\]

Where \(\text{fitbest}\) and \(\text{fitworst}\) are the best and the worst fitness of all particles, respectively; \(\text{fit}(i)\) represents the fitness of the agent \(i\); and \(N\) is the total number of CPs. The separation distance \(r_{i,j}\) between two charged particles is defined as follows:

\[
r_{i,j} = \frac{||X_i - X_j||}{|| (X_i + X_j)/2 - X_{best}|| + \epsilon}
\]

where \(X_i\) and \(X_j\) are respectively the positions of the \(i\)th and \(j\)th CPs, \(X_{best}\) is the position of the best current CP, and \(\epsilon\) is a small positive number. Here, \(p_{i,j}\) is the probability of moving each CP towards the others and is obtained using the following function:

\[
p_{i,j} = \begin{cases} 
1 & \text{if } \frac{\text{fit}(i) - \text{fitbest}}{\text{fit}(j) - \text{fit}(i)} > \text{rand} \wedge \text{fit}(j) > \text{fit}(i) \\
0 & \text{else}
\end{cases}
\]

In Eq. (1), \(ar_{i,j}\) indicates the kind of force and is defined as

\[
ar_{i,j} = \begin{cases} 
1 & \text{if } \text{rand} > 0.8 \\
0 & \text{else}
\end{cases}
\]

**Step 3: Solution construction.** Each CP moves to the new position and the new velocity is
calculated as
\[ X_{j,\text{new}} = \text{rand}_{j,1} K_a F_j + \text{rand}_{j,2} K_v V_{j,\text{old}} + X_{j,\text{old}} \]  
(6)

\[ V_{j,\text{new}} = X_{j,\text{new}} - X_{j,\text{old}} \]  
(7)

where \( K_a \) is the acceleration coefficient; \( K_v \) is the velocity coefficient to control the influence of the previous velocity; and \( \text{rand}_{j,1} \) and \( \text{rand}_{j,2} \) are two random numbers uniformly distributed in the range \((0,1)\). In this paper \( K_a \) and \( K_v \) are taken as:

\[ K_a = 1 + \frac{\text{iter}}{\text{iter}_{\text{max}}} \quad \text{and} \quad K_v = 1 - \frac{\text{iter}}{\text{iter}_{\text{max}}} \]  
(8)

Where \( \text{iter} \) is the iteration number, and \( \text{iter}_{\text{max}} \) is the maximum number of iterations.

**Step 4: Updating process.** If a new CP exits from the allowable search space, a harmony search-based handling approach [9] is used to correct its position. In addition, if some new CP vectors are better than the worst ones in the CM, these are replaced by the worst ones in the CM.

**Step 5: Termination criterion control.** Steps 2-4 are repeated until a termination criterion is satisfied [8].

### 3. PARTICLE SWARM OPTIMIZATION

The PSO is based on a metaphor of social interaction such as bird flocking and fish schooling, and is developed by Eberhart and Kennedy [9]. The PSO simulates a commonly observed social behavior, where members (particles) of a group (swarm) tend to follow the lead of the best of the group. In other words, the particles fly through the search space and their positions are updated based on the best positions of individual particles denoted by \( p^k_i \) and the best position among all particles in the search space represented by \( p^g_i \).

The procedure of the PSO is reviewed below:

**Step 1:** Initialization. An array of particles and their associated velocities are initialized with random positions.

**Step 2:** Local and global best creation. The initial particles are considered as the first local best and the best of them corresponding to the minimum objective function will be the first global best.

**Step 3:** Solution construction. The velocity and location of each particle are changed to the new position using the following equations:

\[ X_i^{k+1} = X_i^k + V_i^{k+1} \]  
(9)

\[ V_i^{k+1} = \omega V_i^k + C_1 r_1 \xi_1( P_i^k - X_i^k ) + C_2 r_2 \xi_2( P^g_i - X_i^k ) \]  
(10)
Where \( X_i^k \) and \( V_i^k \) are the position and velocity for the \( i \)th particle at iteration \( k \); \( \omega \) is an inertia weight to control the influence of the previous velocity; \( r_1 \) and \( r_2 \) are two random numbers uniformly distributed in the range of \((0, 1)\); \( c_1 \) and \( c_2 \) are two acceleration constants; \( p_i^k \) is the best position of the \( i \)th particle up to iteration \( k \); \( p_g^k \) is the best position among all particles in the swarm up to iteration \( k \) and the sign “\( \circ \)” denotes element-by-element multiplication.

**Step 4:** Local best updating. The objective function of the particles is evaluated and \( p_i^k \) is updated according to the best current value of the fitness function.

**Step 5:** Global best updating. The current global minimum objective function value among the current positions is determined and thus \( p_g^k \) is updated if the new position is better than the previous one.

**Step 6:** Terminating criterion control. Step 3 to Step 5 are repeated until a terminating criterion is satisfied [9].

### 4. GEOMETRICAL MODEL OF ARCH DAM

#### 4.1. Shape of the central vertical section

The shape of an arch dam has two basic characteristics, namely the curvature and thickness. Both the curvature and the thickness change both in horizontal and vertical directions. For the central vertical section of double-curvature arch dam, as shown in Figure 1, one polynomial of \( n \)th order is used to determine the curve of upstream boundary and another polynomial is employed to determine the thickness. In this study, a parabolic function is considered for the curve of upstream face as [12]:

\[
y(z) = b(z) = -sz + \frac{s z^2}{2 \beta h}
\]

where \( h \) and \( s \) are the height of the dam and the slope at crest respectively, and the point where the slope of the upstream face equals to zero is \( z = \beta h \) in which \( \beta \) is constant.

![Figure 1. Central vertical section of an arch dam](image-url)
\[ t_1(z) = n_1(z) t_{c1} + n_2(z) t_{c2} + n_3(z) t_{c3} \]  (12)

Where

\[ n_1(z) = \frac{(\frac{z}{h} - \lambda)(\frac{z}{h} - 1)}{\lambda}, \quad n_2(z) = \frac{\frac{z}{h} - 1}{\lambda(\lambda - 1)}, \quad n_3(z) = \frac{(\frac{z}{h} - \lambda)(\frac{z}{h})}{(1 - \lambda)} \]  (13)

in which \( t_{c1}, t_{c2} \) and \( t_{c3} \) are the thicknesses of the central vertical section at \( z=0, z=\lambda h \) and \( z=h \), respectively and \( \lambda \) is a factor in the range of \((0,1)\) and in this study is considered as \( \lambda=0.55 \).

### 4.2. Shape of the horizontal section

As shown in Figure 2, for the purpose of symmetrical canyon and arch thickening from crown to abutment, the shape of the horizontal section of a parabolic arch dam is determined by the following two parabolas:

**Figure 2. The shape of the horizontal section of a parabolic dam**

At the upstream face of the dam:

\[ y_u(x,z) = \frac{1}{2 r_u(z)} x^2 + b(z) \]  (14)

At the downstream face of the dam:

\[ y_d(x,z) = \frac{1}{2 r_d(z)} x^2 + b(z) + t_c(z) \]  (15)

where \( r_u \) and \( r_d \) are radii of curvatures correspond to upstream and downstream curves respectively, and functions of \( n \)th order with respect to \( z \) can be used for those radii. In this study, \( n=2 \) is assumed, and \( r_u \) and \( r_d \) are considered as quadratic functions:

\[ r_u = n_1 r_{u1} + n_2 r_{u2} + n_3 r_{u3} \]
\[ r_d = n_1 r_{d1} + n_2 r_{d2} + n_3 r_{d3} \]  (16)

where \( r_{u1}, r_{u2}, r_{u3} \) and \( r_{d1}, r_{d2}, r_{d3} \) are values of \( r_u \) and \( r_d \) at \( z=0, z=\lambda h \) and \( z=h \), respectively.
5. VERIFICATION OF THE FINITE ELEMENT MODEL

In order to validate the finite element model with the employed assumptions, an idealized model of Morrow Point arch dam which is located 263 km southwest of Denver, Colorado, is investigated, Figure 3. The properties of the dam in details can be found in Ref. [13]. The physical and mechanical properties involved here are the concrete density \(2483\text{N} \cdot \text{s}^2/\text{m}^4\), the concrete poison’s ratio \(0.2\) and the concrete elasticity \(27580 \times 10^4\ \text{MPa}\). It is assumed that the reservoir is empty and dam foundation is rigid.

In literature, the natural frequencies of some modes are eliminated due to considering only half of the dam. Thus, in order to perform an exact analysis, it is necessary to consider the complete dam. In the present work complete model is considered and the first three natural frequencies of the mode of Morrow Point dam are determined from the frequency response function for the crest displacement and the results are compared to those reported in the literature [13-14]. The natural frequencies from the other literatures and present work are given in Table 1. It can be observed that a good conformity is achieved between the results of
present work with those of the previously reported results.

<table>
<thead>
<tr>
<th></th>
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</thead>
<tbody>
<tr>
<td>1</td>
<td>4.27</td>
<td>4.29</td>
<td>4.28</td>
</tr>
<tr>
<td>2</td>
<td>-</td>
<td>-</td>
<td>4.59</td>
</tr>
<tr>
<td>3</td>
<td>-</td>
<td>6.71</td>
<td>6.78</td>
</tr>
</tbody>
</table>

6. ARCH DAM OPTIMIZATION

6.1. Mathematical model and optimization variables

The optimization problem can formally be stated as follows:

\[
\begin{align*}
    \text{Find} & \quad X = [x_1, x_2, x_3, ..., x_n] \\
    \text{to minimize} & \quad Mer(X) = f(X) \times f_{\text{penalty}}(X) \\
    \text{subjected to} & \quad g_i(X) \leq 0, \quad i = 1, 2, \ldots, m \\
    & \quad x_{\text{imin}} \leq x_i \leq x_{\text{imax}} 
\end{align*}
\]

where \( X \) is the vector of design variables with \( n \) unknowns, \( g_i \) is \( i \)th constraint from \( m \) inequality constraints and \( Mer(X) \) is the merit function; \( f(X) \) is the cost; \( f_{\text{penalty}}(X) \) is the penalty function which results from the violations of the constraints corresponding to the response of the arch dam. Also, \( x_{\text{imin}} \) and \( x_{\text{imax}} \) are the lower and upper bounds of design variable vector.

Exterior penalty function method is employed to transform the constrained dam optimization problem into an unconstrained one as follows:

\[
    f_{\text{penalty}}(X) = 1 + \gamma_p \sum_{i=1}^{m} \max(0, g_i(X))^2
\]

where \( \gamma_p \) is penalty multiplier.

6.2. Design variables

The most effective parameters for creating the arch dam geometry were mentioned in Section 2. The parameters can be adopted as design variables:

\[
    X^T = \{ s, \beta, t_{c1}, t_{c2}, t_{c3}, r_{u1}, r_{u2}, r_{u3}, r_{d1}, r_{d2}, r_{d3} \}
\]
6.3. Design constraints

Design constraints are divided into some groups including the behavioral, geometrical and stability constraints. The behavioral constraints are the restricted natural frequencies that are defined as follows:

\[ f_{rl_n} \leq f_{r_n} \leq f_{ru_n} \Rightarrow \begin{cases} 1 - \frac{f_{r_n}}{f_{rl_n}} \leq 0 \\ \frac{f_{r_n}}{f_{ru_n}} - 1 \leq 0 \\ n = 1, 2, \ldots, n_f \end{cases} \]  

(20)

where \( f_{r_n} \), \( f_{rl_n} \) and \( f_{ru_n} \) are the \( n \)th natural frequency, lower bound and upper bound of the \( n \)th natural frequency, respectively. Also, \( n_f \) is the number of natural frequencies. The most important geometrical constrains are those that prevent from intersection of upstream face and downstream face as:

\[ r_{dn} \leq r_{un} \Rightarrow \frac{r_{dn}}{r_{un}} - 1 \leq 0, \quad n = 1, 2, 3 \]  

(21)

where \( r_{dn} \) and \( r_{un} \) are the radii of curvatures at the down and upstream faces of the dam in \( n \)th position in \( z \) direction. The geometrical constrain that is applied to facilities the construction, is defined as:

\[ s \leq s_{all} \Rightarrow \frac{s}{s_{all}} - 1 \leq 0 \]  

(22)

where \( s \) is the slope of overhang at the downstream and upstream faces of dam and \( s_{all} \) is its allowable value. Usually \( s_{all} \) is taken as 0.3. The constraints ensuring the sliding stability of the dam may be expressed as:

\[ \phi_i \leq \phi \leq \phi_u \]  

(23)

where \( \phi \) is the central angle of arch dam and usually \( 90 \leq \phi \leq 110 \), Ref. [15]

6.4. Cost function

The cost function is the construction cost of the dam, which may be expressed as:

\[ f( X ) = p_v( X ) + p_a( X ) \]  

(24)

where \( v(X) \) and \( a(X) \) are the concrete volume and the casting area of dam body. The unit price of concrete and casting are chosen as \( pv=33.34 \$ \) and \( pa=6.67 \$, respectively.

The volume of concrete can be determined by integrating from dam surfaces as:

\[ v( X ) = \iint_{\text{Area}} [y_a( x, z ) - y_u( x, z )] \, dx \, dz \]  

(25)
in which \( Area \) is an area produced by projecting of dam on \( xz \) plane. The areas of casting can be approximately calculated by summing of the areas of upstream and downstream faces as follows:

\[
\alpha(X) = a_u(X) + a_d(X) = \int \int \int \left[ 1 + \left( \frac{dy}{dx} \right)^2 + \left( \frac{dy}{dz} \right)^2 \right] dx dz + \int \int \int \left[ 1 + \left( \frac{dy}{dx} \right)^2 + \left( \frac{dy}{dz} \right)^2 \right] dy dx dz \quad (26)
\]

where \( a_u \) and \( a_d \) are the casting areas of upstream and downstream faces, respectively [16].

To evaluate \( v(X) \) and \( a(X) \) a computer program is coded using MATLAB [10].

7. NUMERICAL EXAMPLES

In order to assess the effectiveness of proposed procedure and compare with other literature results, a well-known benchmark problem in the field of shape optimization of the arch dam with frequency constraints with a height of 180 m is considered. The width of the valley in its bottom and top are 40 m and 220 m, respectively. A finite element model based on modal analysis for the double-curvature arch dam is presented. The arch dam is treated as a three dimensional linear structure. To mesh of the arch dam body twenty-node isoperimetric solid element is used. It is assumed that the reservoir is empty and dam foundation is rigid to avoid the extra complexities that would otherwise arise. To evaluate the eigenvalues of arch dam a computer program is coded using Opensees [9].

The lower and upper bounds of design variables using empirical design methods are considered as:

\[
\begin{align*}
0 \leq s & \leq 0.3 & \quad 4 \leq t_{cl} & \leq 12 & \quad 50 \leq r_{u1} & \leq 180 & \quad 50 \leq r_{d1} & \leq 180 \\
0 \leq \beta & \leq 1 & \quad 8 \leq t_{cl} & \leq 30 & \quad 40 \leq r_{u1} & \leq 120 & \quad 40 \leq r_{d1} & \leq 120 \\
12 \leq t_{cl} & \leq 40 & \quad 10 \leq r_{u1} & \leq 50 & \quad 10 \leq r_{d1} & \leq 50
\end{align*}
\quad (27)
\]

In current study, natural frequency constraints are imposed as:

\[
fr_1 \leq 3Hz \quad fr_2 \leq 6Hz \quad fr_3 \leq 7Hz \quad fr_4 \leq 8Hz \quad (28)
\]

Table 2 shows the material properties for this example.Specifications of the CSS and PSO methods are given in Tables 3 to 4. This problem has been investigated by Gholizadeh and Seyedpoor [12] using the GA and VSP algorithm.
Table 2. Material properties of arch dam

<table>
<thead>
<tr>
<th>Property/unit</th>
<th>Value</th>
</tr>
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<tbody>
<tr>
<td>E (Modulus of elasticity)/ MPa</td>
<td>21000</td>
</tr>
<tr>
<td>poison’s ratio</td>
<td>0.2</td>
</tr>
<tr>
<td>ρ (Material density)/ kg/m$^3$</td>
<td>2400</td>
</tr>
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Table 3. Specifications of the CSS method

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Specification</th>
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<tbody>
<tr>
<td>Number of CPs</td>
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</tr>
<tr>
<td>Max acceleration coefficient</td>
<td>1.00</td>
</tr>
<tr>
<td>Max velocity coefficient</td>
<td>0.50</td>
</tr>
<tr>
<td>Min acceleration coefficient</td>
<td>0.50</td>
</tr>
<tr>
<td>Min velocity coefficient</td>
<td>0.00</td>
</tr>
<tr>
<td>Magnitude of $a$</td>
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</tr>
<tr>
<td>Maximum iterations</td>
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Table 4. Specifications of the PSO method

<table>
<thead>
<tr>
<th>Parameter</th>
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<tbody>
<tr>
<td>Swarm size</td>
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<td>Cognitive parameter</td>
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<tr>
<td>Social parameter</td>
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<tr>
<td>Inertia weight</td>
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</tr>
<tr>
<td>Maximum iterations</td>
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7.1. Results of optimization

Table 5 represents the design vectors and the cost of the corresponding half the arch dam obtained by different researchers and methods. It can be seen that both CSS and PSO have outperformed their rivals. Also, demonstrate that CSS gives better results than PSO.

Figure 4. The convergence curves for the CSS and PSO
Figure 4 shows the convergence curves for both CSS and PSO for the optimum design of arch dam.

Table 5. Optimum designs of the arch dam obtained by the various methods

<table>
<thead>
<tr>
<th>Variable No.</th>
<th>Gholizadeh &amp; Seyedpoor [12]</th>
<th>Present work</th>
</tr>
</thead>
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<td></td>
<td>GA</td>
<td>VSP</td>
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<table>
<thead>
<tr>
<th></th>
<th>Gholizadeh &amp; Seyedpoor [12]</th>
<th>Present work</th>
</tr>
</thead>
<tbody>
<tr>
<td>cost of the corresponding half the arch dam ($10^6$)</td>
<td>8.740</td>
<td>6.576</td>
</tr>
</tbody>
</table>

8. CONCLUDING REMARKS

In this paper the shape optimization of an arch dam is performed. The cost of the arch dam includes the concrete volume and the casting areas considered as the objective function, with frequency, geometrical and stability constraints. To optimize the arch dam two meta-heuristic algorithms namely the CSS and PSO are utilized. To validate the finite element model, the Morrow Point arch dam is analyzed. It is observed that natural frequencies of some mode are eliminated due to considering only half of the dam in the results reported in the literature.

Form the results of this study it can be seen that both CSS and PSO have performed better than the other methods available in the literature for the examples considered. The solved example demonstrates that the CSS leads to better results than the PSO.

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